

# Exercise Problems - 10

## Functions - 1

1. Write a program that accepts a number  $n$  from the user and prints all prime numbers less than  $n$ , by repeatedly calling the function `isprime()` we discussed in class.
2. Write a program that takes  $n$  numbers from the user and stores them into an array and then computes the maximum of the elements of the array by repeatedly calling the function `maximum()` that we discussed in class. Recall that this function takes two integers as parameters and returns an integer value.
3. In this exercise, we will develop a program that approximately computes  $\cos(x)$  (where  $x$  is in radians), using the formula  $\cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots$ . Write a C function `cos` that takes two parameters, a float variable  $x$  and a positive integer  $k$  and returns a double value which is an approximation of  $\cos(x)$  obtained by summing up the first  $k$  terms of the above series expansion. For example, if  $x = 1.5$  and  $k = 1$ , the return value should be 1 and if  $x = 1.5$  and  $k = 3$ , the return value should be the result of  $1 - \frac{1.5^2}{2!} + \frac{1.5^4}{4!}$ . Write a main function that accepts a value  $x$  and number of terms  $n$  as inputs from the user, invokes the function `cos()` with parameters  $x$  and  $n$  outputs the resultant value to the user. Note that, `cos()` function will be more efficient if you compute every term in the series from its previous term, than recompute each term from the beginning.
4. Write a program that takes a positive number  $n$  and a non-negative number  $k$  as inputs from the user and outputs the value of  $nP_k$ . To implement this, write a function `CountPermut` which takes two parameters  $n$  and  $k$  and computes  $nP_k$  using the formula

$$nP_k = n \times (n-1) \times \dots \times (n-k+1)$$

and returns this value. Your main function should take inputs from the user, do necessary validations and call the function `CountPermut` to compute the result, and then outputs the result to the user.

5. Rewrite the above program by redefining the `CountPermut` function to be a recursive function, which uses the formula:

$$nP_k = 1, \text{ if } k = 0 \text{ and } nPk = nP_{k-1} \times n - k + 1, \text{ otherwise.}$$

Make sure that your function terminates for all possible combinations of input values.